Thermal conductivity and thermal diffusivity of cores from a 26 meter deep borehole drilled in Livingston Island, Maritime Antarctic

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1. Introduction

Thermal conductivity is one of the major factors that affect the temperature distribution in the ground. As a result of different thermal conductivities in the ground its thermal structure may change laterally as well as vertically. On the other hand, thermal diffusivity, which controls the rate at which heat dissipates through a material, is also important in processes where temperature changes with time. Even though there is agreement about the importance of those two physical properties of rocks in the study of the thermal regime of the ground, not many measurements have been performed on rocks of permafrost areas. In contrast with the thermal conductivity and the thermal diffusivity, the heat generated by radioactive decay in rocks has an effect of about 20 to 50% in the temperature distribution in the ground (Blackwell and Steele, 1989); however, the importance of the heat production per unit volume was calculated. The estimated heat production for the first half of the borehole is 2.218 μW/m³ while for the second half it is 2.173 μW/m³; these heat production values are compatible with acidic rock types. Porosity and density were also estimated for the same cores.

The Antarctic Peninsula has a mild and humid climate (King and Turner, 1997; Van de Berg et al., 2008) and has experienced a rapid mean annual air temperature (MAAT) increase of about 2.58 °C over the last 50 years (King, 1994; Turner et al., 2005). It is the only land mass in its latitudinal range and so the knowledge of the atmospheric conditions and related phenomena in the Antarctic Peninsula is important to study changes in the Antarctic climate and atmospheric circulation.

Permafrost evolution and spatial distribution are good indicators of climate change; in the northern part of the Antarctic Peninsula permafrost is often discontinuous. Permafrost areas are also very sensitive to changes in temperature and precipitation and so affects geomorphic processes (Ramos and Vieira, 2003; Ramos et al., 2008a,b).

This short paper presents the results of a study performed on cores obtained in a borehole 26 m deep (Permamod-Gulbenkian 1 — PG1) that was drilled and instrumented in 2008 on the top of Mount Reina...
Soﬁa (275 m a.s.l.) near the Spanish Antarctic Station in Livingston Island, South Shetland Islands (Fig. 1). Since this borehole is intended for long-term permafrost monitoring, this paper describes the physical properties measured in the cores collected from it so that estimates of the past climate evolution can be made and energy processes at permafrost and active layer levels can be studied. Thermal conductivity, thermal diffusivity, heat production, density, and porosity were measured in the cores of PG1 borehole. These data are of particular interest and importance in the case of the Antarctic Peninsula and high latitudes, in general, because the climate change that is occurring will change the surface heat balance as well as the soil temperature and hence the distribution and evolution of permafrost. Furthermore, those properties affect the thermal regime of the permafrost areas and the active layer and so are important to interpret past and present soil temperature.

2. Study site and borehole location

Livingston Island is located at 62°39′S, 60°21′W in the South Shetland Islands. The climate at sea level is cold maritime, with frequent summer rainfall and a moderate annual temperature range. The climate reﬂects the strong inﬂuence of the circum-Antarctic low-pressure system and meteorological conditions in summer are dominated by the continuous inﬂuence of polar frontal systems (Styszynska, 2004). Relative humidity is usually high, with average values of 80–90%. King George Island of the South Shetlands Islands shows a MAAT of −1.6 °C at sea level and an annual precipitation of about 500 mm (Ramos et al., 2009). Permafrost in the South Shetland Islands is widespread above the Holocene raised beaches about 30 m a.s.l. (Serrano and Lopez-Martinez, 2000; Hauck et al., 2007). Air temperatures measured in the Spanish Antarctic Station in Livingston Island, at 15 m a.s.l., show MAATs from year 2000 to year 2006 that range from −3.2 °C to −1.5 °C. From April to November, the average daily temperatures at sea level are generally below 0 °C and from December to March they are generally positive.

In the year 2008 a 26 m deep borehole (PG1 borehole) was drilled in Mount Reina Soﬁa (Fig. 1). Near the site of the borehole the MAAT (2003–2006) was −4.2 °C (Ramos et al., 2008b) and mean annual ground temperatures measured since 2000 (at depths of 15, 25, 40, and 90 cm in a 1.1 m borehole) vary between −2.6 °C and −2.1 °C. The measured active layer thickness, based on direct observations in pits and temperature data, was approximately 70 cm (Ramos et al., 2008a); however, since 2003, the thickness has increased to 90 cm.

Geoelectrical and seismic surveys performed in the area of the PG1 borehole indicate a 0.5–1 m thick unfrozen layer with relatively low electrical resistivities (1000–2000 Ω·m) and low P-wave velocities (500–1000 m/s) above a 3–4 m thick layer with high electrical resistivities (7000–10,000 Ω·m) and medium to high P-wave velocities (2500–5500 m/s) representing weathered shales. Below that layer, electrical resistivities decrease to values of 1500–2000 Ω·m indicating low ice contents in a fairly competent bedrock (Hauck et al., 2007). The 26 m borehole, called Permanmodel-Gulbenkian 1 (PG1) is within the CALM (Circumpolar Active Layer Monitoring) site of the Mount Reina Soﬁa. The above mentioned 1.1 m borehole was drilled in 2000 is about 40 m south of PG1. The coordinates of the PG1 borehole are: N 3048545.4 m, E 634145.1 m, and 272 m a.s.l. in the Universal Transverse Mercantor Coordinate system (UTM) zone 20 south. Fig. 2 is a picture of the site where the borehole was drilled and shows a phase of the drilling process.

3. Methods

The thermal conductivities and the thermal diffusivities of the cores from PG1 borehole were measured in a TCS Lippmann & Rauen Gbr equipment. This equipment allows measuring thermal conductivity and thermal diffusivity of samples or cores as small as 40×40×40 mm³ simultaneously; thermal conductivity accuracy is 3% with a measurement range of 0.2 to 25.0 W/mK, while thermal diffusivity accuracy is 5% with a measurement range of 0.6 to 3.0×10⁻⁶ m²/s. The measurements were performed on dry cores at room temperature. The measuring device consists of a point like heat source that is moved along the core to be measured. The temperatures before and after heating are measured and used to calculate the thermal conductivity; both

Fig. 1. Location of the PG1 borehole (star) in the Reina Soﬁa Mountain near the Spanish Antarctic Station (Station Juan Carlos I) in Livingston Island.
temperatures are measured exactly in line to the scanning line. A third temperature is also measured "off line" to calculate thermal diffusivity. Thermal conductivity and thermal diffusivity measurements require the use of standards during the measurement procedure, which are rock samples with known thermal conductivities and thermal diffusivities (Popov, 1985).

Heat production by radioactive decay was also estimated for the PG1 borehole. A 8192-channel gamma-ray spectrometer Cicero (crystal NaJ(Tl)) was used to determine the contents in uranium, thorium and potassium from the rock material from the borehole. Because about 1 kg of rock material is necessary to determine the contents in uranium, thorium and potassium of a rock sample, which must be ground, and because the cores should not be destroyed for other analysis and future preservation, and also because it is not expected to have high variations of heat production for such a short depth range, it was decided to use chips from two sections of the borehole to obtain the necessary mass of rock material for the analysis; the first section corresponds to a depth interval of 2 to 12 m; the second section corresponds to a depth interval of 12 to 25 m. The heat production (HP) values were calculated using the formula (Schön, 1996):

\[
A = \rho \cdot (0.097 \cdot C_U + 0.027 \cdot C_{Th} + 0.036 \cdot C_K)
\]

where \( A \) is the heat production in \( \mu W/m^2 \), \( \rho \) is the rock sample density in g/cm\(^3\), \( C_U \), \( C_{Th} \), and \( C_K \) are the relative contents in uranium, thorium, and potassium in units as indicated in Table 2. Table 2 also shows the values of the heat production for those two sections along the borehole. The density of 2.7 g/cm\(^3\) was used to calculate the heat production by Eq. (1) in the two above-mentioned sections; that value is the average of the density values estimated for each of the cores in Table 3.

Porosity and density were also estimated for several cores from PG1 borehole using saturation and buoyancy techniques (Franklin et al., 2007). With those porosity values thermal conductivities for the cores filled with water and ice were calculated using the following expression (Beardsmore and Cull, 2001):

\[
\lambda_s = \lambda_m^{1-\phi} \cdot \lambda_p^\phi
\]

where \( \lambda_s \) is the average thermal conductivity of the rock sample, \( \lambda_m^{1-\phi} \) is the thermal conductivity of the rock matrix, and \( \lambda_p^\phi \) is the thermal conductivity of the material that fills the pores (water or ice).

4. Results

From a lithological point of view the cores from the borehole indicate that the section of the borehole to a depth of about 25 m depth is mainly composed of siltstones; from 25 m deep to the bottom of the borehole, the borehole crosses quartz sandstones. Thin sections were prepared and petrographic analysis shows that the silts are well calibrated and in the matrix have quartz grains and several other lithoclasts. The quartz sandstone is composed of feldspar (essentially plagioclase) and calcite crystals.

The values of thermal conductivity measured in the cores can be seen in Table 1 and vary between 2.6 and 3.3 W/mK. The values of thermal diffusivity are also presented in Table 1 and vary between 1.1 \times 10^{-6} and 1.6 \times 10^{-6} m^2/s.

Uranium, thorium and potassium contents as well as the heat production (HP) values (Table 2) for the upper and lower sections of the borehole are, respectively, 2.218 \( \mu W/m^3 \) and 2.173 \( \mu W/m^3 \) which are compatible with acidic rock types.

For completeness, density and porosities are also presented in Table 3 for the same cores as in Table 1, as well as the thermal conductivity values corrected for the pores filled with air (dry), water and ice.

<table>
<thead>
<tr>
<th>Depth of sample (m)</th>
<th>Thermal conductivity ( \pm 0.1 ) (W/mK)</th>
<th>Thermal diffusivity ( \times 10^{-6} ) ( \pm 0.1 ) (m^2/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.3</td>
<td>2.7</td>
<td>1.1</td>
</tr>
<tr>
<td>5.8</td>
<td>2.6</td>
<td>1.1</td>
</tr>
<tr>
<td>9.6</td>
<td>2.6</td>
<td>1.1</td>
</tr>
<tr>
<td>15.2</td>
<td>2.6</td>
<td>1.1</td>
</tr>
<tr>
<td>20.4</td>
<td>2.7</td>
<td>1.2</td>
</tr>
<tr>
<td>24.3</td>
<td>2.7</td>
<td>1.2</td>
</tr>
<tr>
<td>25.9</td>
<td>3.3</td>
<td>1.6</td>
</tr>
</tbody>
</table>
where \( \text{grad} \ T \) is the geothermal gradient and \( \frac{\partial T}{\partial z} \) where \( T \) is the temperature, \( t \) is the time, \( z \) is the depth, \( T_0 \) is the surface amplitude or the phase lag of the temperature wave at depths \( z_1 \) and \( z_2 \).

\[ \alpha = \sqrt{\frac{2\pi}{\omega}} \left( \frac{z_1 - z_2}{d} \right)^2 \]

function to the temperature data, which can be seen in Fig. 3 for the temperature time series for 3.5 and 6 m depth. As an example, using values from the sinusoid functions of Fig. 3 (which are the best-fit sinusoids to the actual temperature data calculated by the graphing package used to draw the graphs) and Eq. (6) the calculated thermal diffusivity is \( 2.2 \times 10^{-6} \text{ m}^2/\text{s} \), which is about the double of the values measured for depths between 3.5 and 6 m.

### Table 2
Heat production estimates for the upper half and the lower half of the PG1 borehole. Eq. (1) in the text was used to calculate the heat production values.

<table>
<thead>
<tr>
<th>Depth range (m)</th>
<th>Uranium (p.p.m.)</th>
<th>Thorium (p.p.m.)</th>
<th>Potassium (%)</th>
<th>Heat production (A) (W/m²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2–12</td>
<td>3.539</td>
<td>13.199</td>
<td>3.652</td>
<td>2.218</td>
</tr>
</tbody>
</table>

### 5. Thermal diffusivity from temperatures in PG1 borehole

PG1 borehole is cased and a chain of thermistors was installed in it on January 30, 2008; thermistor’s depths are 0.2, 0.4, 0.8, 1.2, 1.6, 2.5, 3, 3.5, 4, 5, 6, 8, 10, 12.5, 15, 17.5, 20, 22.5, and 25 m, and temperature is measured every 5 min; hourly averages (maximum and minimum temperatures) are stored in a datalogger.

The temperature time series read by each thermistor can be used to calculate the thermal diffusivities for different depths (Carslaw and Jaeger, 1959; Horton et al., 1983; Hurley and Wiltshire, 1993). If we assume that heat transfer is only by conduction in the vertical direction, and the ground is homogeneous and isotropic, thermal diffusivity \( \alpha \) can be calculated from ground temperatures by integrating the heat conduction equation

\[ \frac{\partial T}{\partial t} = \alpha \frac{\partial^2 T}{\partial z^2} \quad (3) \]

with the periodic boundary condition of period \( 2\pi/\omega \)

\[ T(z = 0, t) = T_0 + A_0 \sin(\omega t - \epsilon_0), \quad (4) \]

where \( T \) is the temperature, \( t \) is the time, \( z \) is the depth, \( T_0 \) is the surface temperature, \( A_0 \) and \( \epsilon_0 \) are, respectively, the amplitude and the phase of the surface wave temperature. The distribution of temperature as a function of time and depth is

\[ T(z, t) = T_0 + z \text{grad} T + A_0 e^{-z^2/d} \sin(\omega t - z/d - \epsilon_0) \quad (5) \]

where \( \text{grad} T \) is the geothermal gradient and \( d = \sqrt{2\pi/\omega} \). Eq. (5) can be used to calculate thermal diffusivity within a given layer by using the amplitude or the phase lag of the temperature wave at depths \( z_1 \) and \( z_2 \). As a matter of fact, using the amplitude decrease between those two depths the thermal diffusivity is given by

\[ \alpha = \frac{\omega (z_1 - z_2)^2}{2 \ln(A_1/A_2)} \quad (6) \]

where \( A_1 \) and \( A_2 \) are the amplitudes of the temperature wave at depths \( z_1 \) and \( z_2 \), respectively, and \( \alpha \) is the thermal diffusivity in the depth interval \( z_1 \) to \( z_2 \). However, to apply Eq. (6) it is necessary to fit a sinusoid to the temperature data, which can be seen in Fig. 3 for the temperature time series for 3.5 and 6 m depth. As an example, using values from the sinusoid functions of Fig. 3 (which are the best-fit sinusoids to the actual temperature data calculated by the graphing package used to draw the graphs) and Eq. (6) the calculated thermal diffusivity is \( 2.2 \times 10^{-6} \text{ m}^2/\text{s} \), which is about the double of the values measured for depths between 3.5 and 6 m.

### 6. Discussion

From all the properties presented in Tables 1, 2 and 3, thermal conductivity and thermal diffusivity are the essential ones to describe and understand the thermal regime of the ground. This is particularly important in permafrost areas where climatic change is imposing fast changes in permafrost evolution and spatial distribution. In general terms the measured values for the thermal conductivity vary from 2.6 to 3.3 W/mK (see Table 1) with the highest value for the measurement performed in the deepest core. This result is consistent with the fact that below the depth of 25 m the borehole traverses quartz sandstones. The same behavior is observed for the thermal diffusivity: the measured values vary from \( 1.1 \times 10^{-6} \) to \( 1.6 \times 10^{-6} \text{ m}^2/\text{s} \) (see Table 1), with the highest thermal diffusivity measured in the core obtained from the deepest portion of the borehole. Because the area where the PG1 was drilled goes through freezing and thawing processes during the year, estimates of thermal conductivity with the pores filled with air, water and ice were also done. Even though porosity is small for the rock of the cores, there is a significant change in their thermal conductivity, the highest values obtained for the pores filled with ice, as should be expected.

An interesting result emerges from the comparison between the thermal diffusivity values that were measured in the cores and the values that were obtained by using the theory of heat conduction briefly presented in Section 5. Only for the depth range of 3.5–6.0 m, the difference between those values is about the double. Since the temperatures in that section of the borehole are lower than 0 °C (Fig. 4), the difference cannot be a result of thawing and freezing in that layer. The explanation must be looked for in the layers above 3.5 m and on the physical processes occurring in the active layer, i.e., in the energy balance that takes place at the surface of the

### Table 3
Density and porosity of the cores where thermal conductivity and thermal diffusivity were measured (Table 1). T.C. air, T.C. water, and T.C. ice refer to thermal conductivities of the cores with the pores filled with air (measured), with water (calculated using Eq. (2)), and with ice (calculated using Eq. (2)).

<table>
<thead>
<tr>
<th>Core depth (m)</th>
<th>Density (kg/m³)</th>
<th>Porosity (%)</th>
<th>T.C. air (±0.1) (W/mK)</th>
<th>T.C. water (W/mK)</th>
<th>T.C. ice (W/mK)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.3</td>
<td>2700</td>
<td>2.3</td>
<td>2.7</td>
<td>2.9</td>
<td>2.9</td>
</tr>
<tr>
<td>5.8</td>
<td>2704</td>
<td>2.1</td>
<td>2.6</td>
<td>2.7</td>
<td>2.8</td>
</tr>
<tr>
<td>9.6</td>
<td>2715</td>
<td>1.5</td>
<td>2.6</td>
<td>2.7</td>
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<td>2.0</td>
<td>3.3</td>
<td>3.5</td>
<td>3.6</td>
</tr>
</tbody>
</table>

Fig. 3. Time series temperature at 3.5 and 6.0 m depths. Dashed lines are the best fit sinusoids to the temperature data. The coincidence is not very good and the probable explanation for this lack of coincidence must be a result of what happens at shallower depths, in the active layer of the area where the borehole is located. However, the conductive character of the downward propagation of the periodic signal is obvious from the amplitude attenuation and the phase delay.
ground. More research on the measurement of thermal properties at temperatures lower than 0 °C as well as a more detailed analysis of temperature changes at the surface of the ground will be attempted in the future.

At the time this paper is being written, there is no possibility of estimating the heat flow density. As a matter of fact the data obtained up to now are not clear in terms of calculation of the background or deep geothermal gradient, which is fundamental to calculate the heat flow density. The calculation of those two quantities will be attempted in the near future after downloading the latest temperature information in the Antarctica campaign of 2011 which is starting now.

Heat production is also important to understand the thermal regime in the ground and to extrapolate temperatures to depths not reached by boreholes. With that in mind heat production was estimated for two sections in the PG1 borehole, as described in the previous section. The calculated values (2.218 μW/m² for the first half of the borehole and 2.173 μW/m² for the second half) are consistent with values found in other regions of the globe for shales. However, they are too high for the quartz sandstone found in the last meter of the borehole; this results from the fact that only a small portion of the sandstone was present in the mixture of chips coming from a depth range of 12 to 25 m.

Heat flow determinations and inversion of temperature logs from the borehole for climate change evaluation were not possible to do; new data from the summer campaign to start at the time of the writing of this paper will probably allow that calculation.

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